

**SVS 339 B - 15**  
**B.Sc. Vth Semester Degree Examination**  
**Mathematics**  
**(Differential Equation - II)**  
**Paper : 5.2**

Time : 3 Hours

Maximum Marks : 80

**Instructions to Candidates:**

Answer all the sections

**I.** Answer any ten questions. Each question carries 2 marks. **(10×2=20)**

1. Using generating function for Legendre's polynomials  $p_n(x)$  Prove that  
$$P_n(-x) = (-1)^n P_n(x)$$
2. Show that  $J_0'(x) = -J_1(x)$
3. Show that  $J_{-1/2}(x) = \sqrt{\frac{2}{\pi x}} \cdot \cos x$
4. From recurrence relation show that  $J_2(x) = J_0''(x) - \frac{1}{x} J_0'(x)$
5. Show that  $\int_a^b x J_0(ax) dx = \frac{b}{a} J_1(x)$
6. Verify the condition for Integrability of the equation  $yzdx - 2xzdy + (xy - zy^3)dz = 0$
7. Solve  $\frac{xdx}{y^2z} = \frac{dy}{xz} = \frac{dz}{yz}$
8. Define partial differential equation and give one example of first order.
9. Form the Partial differential equation by eliminating arbitrary constants a & c from  
$$x^2 + y^2 + (z - c)^2 = a^2$$
10. Solve  $xp + yq = z$
11. Solve  $p+q=pq$
12. Find the complete Integral of  $pe^y = qe^x$

### SECTION - B

**II. Answer any FIVE**

(5×6=30)

1. Prove that  $p_n(x) = \frac{1}{2^n n!} \frac{d^n}{dx^n} (x^2 - 1)^n$ .
2. Expand  $f(x) = x^4$  in a series of Legendre polynomial of the form  $\sum_{n=0}^{\infty} C_n P_n(x)$ .
3. using recurrence relation  $\frac{d}{dx} [x^n J_n(x)] = x^n J_{n-1}(x)$
4. Using recurrence relation show that  $J_n(x) = \frac{x}{2n} [J_{n-1}(x) + J_{n+1}(x)]$ .
5. Verify the condition for Integrability and solve the equation.  $(y^2 + yz)dx + (xz + z^2)dy + (y^2 - xy)dz = 0$
6. Solve  $\frac{dx}{z(x+y)} = \frac{dy}{z(x-y)} = \frac{dz}{x^2 + y^2}$
7. Solve  $\frac{dx}{z} = \frac{dy}{-z} = \frac{dz}{z^2 + (x+y)^2}$

### SECTION - C

**III. Answer any Five**

(5×6=30)

1. Form the partial differential equation by eliminating arbitrary function f & g from  

$$z = \frac{1}{y} [f(x+ay) + g(x-ay)]$$
  2. Solve the Lagrange's equation  $(x^2 - yz)p + (y^2 - zx)q = z^2 - xy$
  3. Solve  $z^2(p^2x^2 + q^2) = 1$
  4. Solve  $x^2 p^2 + y^2 q^2 = z^2$
  5. Solve  $(p^2 + q^2)z = x^2 - y^2$
  6. Find the complete Integral of  $P^2x + q^2y = z$  by charpits method.
  7. Find the complete Integral of  $px + qy + pq = 0$  by charpits method.
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